

1. **Statistics of integrate-and-fire neurons** For the following use different variants of the leaky integrate-and-fire models provided in `lifspikes.m`, `lifouspikes.m`, and `lifadaptspikes.m` do generate some spike train data. Use the functions you wrote for the Poisson process to analyze the statistics of the spike trains.

- (a) Generate a few trials of the two models for two different inputs that result in qualitatively different spike trains and display them in a raster plot. Decide for a noise strength (good values to try are 0.001, 0.01, 0.1, 1).
- (b) The inverse Gaussian describes the interspike interval distribution of a PIF driven with white noise:

$$p(T) = \frac{1}{\sqrt{4\pi DT^3}} \exp \left[-\frac{(T - \langle T \rangle)^2}{4DT\langle T \rangle^2} \right]$$

where $\langle T \rangle$ is the mean interspike interval and

$$D = \frac{\langle (T - \langle T \rangle)^2 \rangle}{2\langle T \rangle^3}$$

is the diffusion coefficient (variance of the interspike intervals T divided by two times the mean cubed). Show in two plots how this distribution depends on $\langle T \rangle$ and D .

- (c) Extend your function plotting an interspike interval histogram to also report the diffusion coefficient D .
- (d) Compare interspike interval histograms obtained from the LIF and PIF models with the inverse Gaussian.
- (e) Plot the firing rate (inverse mean interspike interval), mean interspike interval, the corresponding standard deviation, CV, and diffusion coefficient as a function of the input to the LIF and the PIF with noise strength set to 0.01.
- (f) Plot the firing rate as a function of input of the LIF and the PIF for various values of the noise strength.
- (g) Use the functions for computing serial correlations, count statistics and fano factors to further explore the statistics of the integrate-and-fire models!